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Name:

The symbol for the rational numbers is \mathbb{Q} while the symbol for the irrational numbers is $\mathbb{R} \setminus \mathbb{Q}$.
So you can express that x is an irrational number by $x \notin \mathbb{Q}$ or by $x \in \mathbb{R} \setminus \mathbb{Q}$.
Recall for any sets R and Q , the set R set minus Q is the set $R \setminus Q \stackrel{\text{def.}}{=} \{x \in R : x \notin Q\}$.
Note the difference in direction in the slash for set minus ($R \setminus Q$) and quotient of numbers ($1/2 = 0.5$).

A symbol for the positive real numbers is $\mathbb{R}^{>0}$ where $\mathbb{R}^{>0} = \{x \in \mathbb{R} : x > 0\}$.
You may use the fact we showed in class that if p is a prime then \sqrt{p} is irrational.

- . **Conjecture A.** For each positive real number x , if x is irrational, then x^2 is irrational.
1. Symbolically write Conjecture A.
 2. State whether Conjecture A is true or false.
 3. Justify your answer to the previous part. You should understand that this means the following. If Conjecture A is true, then provide a proof of Conjecture A. If Conjecture A is false, then provide a counterexample and clearly explain why the counterexample is indeed a counterexample.

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