

Explorations and Activities Exercise

Before stating this homework, review the [Symbolically Write Guidelines](#), which is also posted on the course homework page. It will answer many of the questions you might otherwise have.

- Hint. The phrase *provided that* is used in definitions and can be thought of as saying *if and only if*.
- Hint. For parts 1 and 2, when asked to symbolically complete a sentence started in English, your answer should be of the form $(\forall x \in U)[P(x)]$ or $(\exists x \in U)[P(x)]$ for some properly chosen universe U (e.g., \mathbb{R} , A) and some open sentence $P(x)$, which should contain the variable x and might contain the: number b , set A .
- ▷. Definition 14 will be presented and explored (much more in depth) in Math 554 (*Analysis*) and was used (perhaps unknowingly) in calculating limits in Calculus.
- Def. **Definition 14.** Let A be a subset of the real numbers. The number $b \in \mathbb{R}$ is called an upper bound for the set A provided that for each element $x \in A$, we have $x \leq b$.
- . Using Definition 14, complete the parts of this exercise.
1. Symbolically complete the following sentence (which is started in English). Box your answer.
Let $A \subseteq \mathbb{R}$. The number b is called an upper bound for the set A provided that ...
 2. Symbolically complete the following sentence (which is started in English). Box your answer.
Let $A \subseteq \mathbb{R}$. The number b is not an upper bound for the set A provided that ...
 3. Without using the quantifier symbols, complete the following sentence in English. Box your answer.
You can use math symbols similar to those in Definition 14.
Let $A \subseteq \mathbb{R}$. The number b is not an upper bound for the set A provided that ...
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