

Before stating this ER, review the (linked) [Symbolically Write Guidelines](#), which is also posted on the course homework page. It will answer many of the questions you might otherwise have.

►. Consider the following statement.

$$(\exists x \in \mathbb{Q}) \left[\sqrt{2} < x < \sqrt{3} \right]. \tag{O}$$

1. Write the statement in (O) as an English sentence. Hint. See (linked) [Writing Guidelines](#) to recall that your English sentence should not contain a quantified symbol (e.g., \forall , \exists) nor a logical connective symbol (e.g., \wedge , \vee , \implies , \iff , \sim , \neg); however, it is fine to use math symbols such as: $+$, $=$, $<$, \leq .
2. Symbolically write an equivalent formulation of the statement in (O) as to have a logical connective and 2 separate inequalities. Hint. Fill in the box with a logical connective: \wedge , \vee , \implies , \iff , \sim . Listening to myself carefully as you talk to myself tells me that $\sqrt{2} < x < \sqrt{3}$ can be expressed as: $(\sqrt{2} < x) \square (x < \sqrt{3})$.
3. Symbolically write a useful negation of the statement in (O) that does not use the negation symbol (i.e. \sim or \neg). Box your answer. Hint. DeMorgan. So do you want to start with (O) or your answer to part 2?
4. Write a useful negation of the statement in (O) as an English sentence. Box your answer. (Hint. Same hint as in part 1.)

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