

►. For each problem below do the following.

- a. Express the statement in English without using variables (so can not have an x nor a y). E.g.,
5a. The statement says that there is a real number that is strictly less than every other real number.
- b. Explain, in such a way as to indicate you understand, the indicated validity (true/false-ness) of the statement. You may use, without proof, properties of \mathbb{R} you know from high school. For example, you may use Lemma 1 (without proof).

Lemma 1. If $a \geq 0$ and $b \geq 0$ then $ab \geq 0$.

- 1. Explain why the statement $(\forall x \in \mathbb{R})[x^2 \geq 0]$ is true.
- 2. Explain why the statement $(\exists x \in \mathbb{R})[x^2 < 0]$ is false.
- 3. Explain why the statement $(\exists y \in \mathbb{R})[17 < y]$ is true.
- 4. Explain why the statement $(\forall x \in \mathbb{R})(\exists y \in \mathbb{R})[x < y]$ is true.
- 5. Explain why the statement $(\exists x \in \mathbb{R})(\forall y \in \mathbb{R})[x < y]$ is false.

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