

NOTE Different techniques of integration may produce answers that appear to differ from those shown here; if both are correct, they of course differ only by a constant.

1. $2 \arctan \sqrt{x} + C$

3. $\ln|\sec x| + C$

5. $\frac{1}{2} \sec^2 \theta + C$

7. $x \tan x - \frac{1}{2}x^2 + \ln|\cos x| + C$

9. $\frac{2}{15}(2-x^3)^{5/2} - \frac{4}{9}(2-x^3)^{3/2} + C$

11. $\frac{1}{2}x(25+x^2)^{1/2} - \frac{25}{2} \ln|x+(25+x^2)^{1/2}| + C$

13. $\frac{2}{3}\sqrt{3} \arctan \frac{1}{3}\sqrt{3}(2x-1) + C$

15. $\frac{103}{87}\sqrt{29} \arctan \frac{1}{29}\sqrt{29}(3x-2) + \frac{5}{6} \ln(9x^2-12x+33) + C$

17. $\frac{2}{3} \arctan(\frac{1}{3} \tan \frac{1}{2}\theta) + C$

19. $\arcsin(\frac{1}{2} \sin x) + C$

21. $-\ln|\ln \cos x| + C$

23. $(1+x) \ln(1+x) + C - \checkmark$

25. $\frac{1}{2}x(x^2+9)^{1/2} + \frac{3}{2} \ln|x+(x^2+9)^{1/2}| + C$

27. $\frac{1}{2}(x-1)(2x-x^2)^{1/2} + \frac{1}{2} \arcsin(x-1) + C$

29. $\frac{1}{3}x^3 + 2x - \sqrt{2} \ln\left|\frac{x+\sqrt{2}}{x-\sqrt{2}}\right| + C$

31. $\frac{1}{2}(x^2+x)(x^2+2x+2)^{-1} - \frac{1}{2} \arctan(x+1) + C$

33. $\frac{1}{2} \tan \theta + C \text{ or } \frac{1}{2} \frac{\sin 2\theta}{1+\cos 2\theta} + C$

35. $\frac{1}{3} \sec^5 x - \frac{1}{3} \sec^3 x + C$

37. $\frac{1}{8}x^2[4(\ln x)^3 - 6(\ln x)^2 + 6(\ln x) - 3] + C$

39. $\frac{1}{2}e^x(1+e^{2x})^{1/2} + \frac{1}{2} \ln[e^x + (1+e^{2x})^{1/2}] + C$

41. $\frac{1}{54} \operatorname{arcsec} \frac{1}{3}x + \frac{1}{18}x^{-2}(x^2-9)^{1/2} + C$

43. $\ln|x| + \frac{1}{2} \arctan 2x + C$

45. $\frac{1}{2}(\sec x \tan x - \ln|\sec x + \tan x|) + C$

47. $\ln|x+1| - \frac{2}{3}x^{-3} + C$

49. $\ln|x-1| + \ln(x^2+x+1) + (x-1)^{-1} - 2(x^2+x+1)^{-1} + C$

51. $\frac{1}{3} \ln \left| \frac{1-\cos \theta + 3\sin \theta}{1-\cos \theta - 3\sin \theta} \right| + C$

53. $\frac{1}{3}(\arcsin x)^3 + C$

55. $\frac{1}{2} \sec^2 z + \ln|\cos z| + C$

57. $\frac{1}{2} \arctan(e^{x^2}) + C$

59. $-\frac{1}{2}(x^2+1) \exp(-x^2) + C$

61. $-x^{-1} \arcsin x - \ln \left| \frac{1+(1-x^2)^{1/2}}{x} \right| + C$

63. $\frac{1}{8} \arcsin x + \frac{1}{8}x(2x^2-1)(1-x^2)^{1/2} + C$

65. $\frac{1}{4} \ln|2x+1| + \frac{2}{3}(2x+1)^{-1} + C$

67. $\frac{1}{2} \ln|e^{2x}-1| + C$

69. $2 \ln|x+1| + 3(x+1)^{-1} - \frac{5}{3}(x+1)^{-3} + C$

71. $\frac{1}{2} \ln(x^2+1) + \arctan x - \frac{1}{2}(x^2+1)^{-1} + C$

73. $\frac{1}{45}(x^3+1)^{3/2}(6x^3+4) + C$

75. $\frac{2}{3}(1+\sin x)^{3/2} + C$

77. $\frac{1}{2} \ln|\sec x + \tan x| + C$

79. $-2(1-\sin t)^{1/2} + C$

81. $-2x + \sqrt{3} \arctan \frac{1}{3}\sqrt{3}(2x+1)$

$+ \frac{1}{2}(2x+1) \ln(x^2+x+1) + C$

83. $-x^{-1} \arctan x + \ln|x(1+x^2)^{-1/2}| + C$

85. $\frac{1}{2} \ln(x^2+1) + \frac{1}{2}(x^2+1)^{-1} + C$

87. $\frac{1}{2}(x-6)(x^2+4)^{-1/2} + C$

89. $\frac{1}{3}(1+\sin^2 x)^{3/2} + C$

91. $\frac{1}{2}e^x(x \sin x - x \cos x + \cos x) + C$

93. $-\frac{1}{2}(x-1)^{-2} \arctan x + \frac{1}{2}(x^2+1)(x-1)^{-2} - \frac{1}{4}(x-1)^{-1} + C$

95. $\frac{11}{9} \arcsin \frac{1}{2}(3x-1) - \frac{2}{9}(3+6x-9x^2)^{1/2} + C$

97. $\frac{1}{2} \cos^2 \theta + \cos \theta + C$

99. $x \operatorname{arcsec} \sqrt{x} - (x-1)^{1/2} + C$

101. $\frac{1}{4}\pi(e^2 - e^{-2} + 4)$

103. (a) $A_b = \pi \left(\sqrt{2} - e^{-b}(1+e^{-2b})^{1/2} + \ln \left[\frac{1+\sqrt{2}}{(e^{-b}+(1+e^{-2b})^{1/2})} \right] \right);$
(b) $\pi[\sqrt{2} + \ln(1+\sqrt{2})] \approx 7.2118$

105. $\frac{1}{2}\pi\sqrt{2} \left[2\sqrt{14} - \sqrt{2} + \ln \left(\frac{1+\sqrt{2}}{2\sqrt{2}+\sqrt{7}} \right) \right],$
approximately 11.66353

109. $\frac{5}{4}\pi \approx 3.29699$

111. The value of the integral is $\frac{1}{630}$.

113. $\frac{1}{2}(5\sqrt{6}-3\sqrt{2}) + \frac{1}{2} \ln \left(\frac{1+\sqrt{2}}{\sqrt{3}+\sqrt{2}} \right) \approx 3.869983$

115. The substitution is $u = e^x$.

(a) $\frac{2}{3}\sqrt{3} \arctan \frac{1}{3}\sqrt{3}(1+2e^x) + C$

119. $\frac{1}{4}\sqrt{2} \ln \left| \frac{1+\tan \theta - (2\tan \theta)^{1/2}}{1+\tan \theta + (2\tan \theta)^{1/2}} \right| - \frac{1}{2}\sqrt{2} \arctan(2 \cot \theta)^{1/2} + C$