Below are just HINTS, without the needed justifications.

Recall that often there is more than one way to determine the behavior of a series.

abs. conv. – absolutely convergent cond. conv. - conditionally convergent divg. – divergent AST – Alternating Series Test CT – Comparison Test LCT – Limit Comparison Test (1) divg. – *p*-series with $p = \frac{1}{2}$ (2) cond. conv. – AST & *p*-series with $p = \frac{1}{2}$ (3) cond. conv. – AST & CT to $\frac{1}{n+1}$ (4) abs. conv. – LCT to $\frac{1}{n^2}$ (5) abs. conv. – ratio test $\rho = 0$ (6) abs. conv. – ratio test $\rho = 0$ (7) abs. conv. – integral test (8) divg. $-n^{th}$ -term test for divergence (9) abs. conv. – root test $\rho = 0$ (10) abs. conv. – LCT to $\left(\frac{1}{n}\right)_{1}^{\frac{3}{2}}$ (11) abs. conv. – CT to $\frac{n'1}{(3n-2)^n}$ & do the root test to $\frac{1}{(3n-2)^n}$ (12) abs. conv. – CT to $\frac{2}{n^2}$. note that $|\arctan n| \leq \frac{\pi}{2}$. (13) abs. conv. – CT to $\left(\frac{1}{n}\right)^{\frac{3}{2}}$. note that $\ln(n!) = \ln(1 \cdot 2 \cdots n) = \ln 1 + \ln 2 + \dots \ln n \le n \ln n$ and so for big n $\frac{\ln(n!)}{n^3} \leq \frac{n \, \ln n}{n^3} = \frac{\ln n}{n^2} \leq \frac{n^{\frac{1}{2}}}{n^2} = \frac{1}{n^{\frac{3}{2}}}$ (14) abs. conv. – ratio test $\rho = 0$ (15) divg. $-n^{th}$ -term test for divergence. note that $\left(\frac{n}{n+1}\right)^n = \left[\left(\frac{n+1}{n}\right)^n\right]^{-1} = \left[\left(1+\frac{1}{n}\right)^n\right]^{-1} \to \left[e^1\right]^{-1} = e^{-1} \neq 0.$