

0B. Volume of Revolutions. Let's say we revolve some region in the xy -plane around an axis of revolution so we get a solid of revolution. Next we want to find the volume of this solid of revolution.

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- In parts a, fill in the blanks with: x or y .
 - In parts b and c, fill in the blanks with a formula involving *some of*:
 2 , π , radius, radius_{big}, radius_{little}, average radius, height, and/or thickness.
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►. **Disk/Washer Method.** Let's find the volume of this solid of revolution using the disk or washer method.

a. If the axis of revolution is:

- the x -axis, or parallel to the x -axis, then we partition the x -axis.
- the y -axis, or parallel to the y -axis, then we partition the y -axis.

b. If we use the **disk method**, then the volume of a typical disk is:

$$\pi (\text{radius})^2 (\text{height})$$

If we use the **washer method**, then the volume of a typical washer is:

$$\pi (\text{radius}_{\text{big}})^2 (\text{height}) - \pi (\text{radius}_{\text{little}})^2 (\text{height}) \quad \text{or} \quad \pi [(\text{radius}_{\text{big}})^2 - (\text{radius}_{\text{little}})^2] (\text{height})$$

c. If we partition the z -axis, where z is either x or y , the $\Delta z =$ height.

►. **Shell Method.** Let's find the volume of this solid of revolution using the shell method.

a. If the axis of revolution is:

- the x -axis, or parallel to the x -axis, then we partition the y -axis.
- the y -axis, or parallel to the y -axis, then we partition the x -axis.

b. If we use the **shell method**, then the volume of a typical shell is:

$$2\pi (\text{average radius}) (\text{height}) (\text{thickness}) \quad \text{or} \quad 2\pi (\text{radius}) (\text{height}) (\text{thickness})$$

c. If we partition the z -axis, where z is either x or y , the $\Delta z =$ thickness or radius_{big} - radius_{little}.