## HAND IN PART

| MARK BOX |  |  |
| :---: | :---: | :--- |
| PROBLEM | POINTS |  |
| 0 | 25 |  |
| $1-7$ | 35 |  |
| 8 | 10 |  |
| 9 | 10 |  |
| 10 | 10 |  |
| 11 | 10 |  |
| $\%$ | 100 |  |

NAME: $\qquad$

PIN: $\qquad$

## INSTRUCTIONS

- On Problem 0, fill in the blanks. As you know, if you do not make at least half of the points on Problem 0, then your score for the entire exam will be whatever you made on Problem 0.
- Problems 1-7 are multiple choice.
- First, indicate (to yourself) your answers directly on the STATEMENT OF MULTIPLE CHOICE PROBLEMS part.
- Once finished with the multiple choice problems, go back to the HAND IN PART and indicate your answers on the table provided.
- You can take the STATEMENT OF MULTIPLE CHOICE PROBLEMS part home with you (so you can check your answers once the solutions are posted).
- For the remaining problems, to receive credit you must:
(1) work in a logical fashion, show all your work, indicate your reasoning; no credit will be given for an answer that just appears;
such explanations help with partial credit
(2) if a line/box is provided, then:
- show you work BELOW the line/box
- put your answer on/in the line/box
(3) if no such line/box is provided, then box your answer.
- Upon request, you will be given as much (blank) scratch paper as you need.
- Check that your copy of the exam has all of the problems.
- During the exam, the use of unauthorized materials is prohibited. Unauthorized materials include: electronic devices, books, and personal notes. Unauthorized materials (including cell phones) must be in a secured (e.g. zipped up, snapped closed) bag placed completely under your desk or, if you did not bring such a bag, given to Prof. Girardi to hold for you during the exam (and they will be returned when you leave the exam). This means no electronic devices (such as cell phones) allowed in your pockets. Please, if I forget, remind me to pull up a clock on the projector screen.
- During this exam, do not leave your seat unless you have permission. If you have a question, raise your hand. When you finish: put your pencil down and raise your hand.
- This exam covers (from Calculus by Stewart, $6^{\text {th }}$ ed., ET):
§7.1-7.5, 7.8, 11.1 .


## 0. Fill in the blanks (each worth 1 point).

- $\int \cos u d u=\square+C$
- $\int \sin u d u=\square+C$
- trig formula ... since $\cos ^{2} \theta+\sin ^{2} \theta=1$, we know that the corresponding relationship beween tangent (i.e., tan) and secant (i.e., sec) is $\qquad$ .
. Integration by parts formula: $\int u d v=$ $\qquad$
- If $a$ is a contant and $a>0$ then $\int \frac{1}{a^{2}+u^{2}} d u=$ $\qquad$ $+C$
- Trig. Substitution:
if the integrand involves $a^{2}+u^{2}$, then one makes the substitution $u=$ $\qquad$
- If $u \neq 0$, then $\int \frac{d u}{u}=\square|u|+C$
- Partial Fraction Decomposition. If one wants to integrate $\frac{f(x)}{g(x)}$ where $f$ and $g$ are polyonomials and [degree of $f] \geq[$ degree of $g]$, then one must first do $\qquad$
- If $a$ is a constant and $a>0$ but $a \neq 1$, then $\int a^{u} d u=$ $\qquad$ $+C$
- $\quad \int \tan u d u=$ $\qquad$ $+C$
- $\quad \int \cot u d u=$ $\qquad$ $+C$
- $\int \sec ^{2} u d u=$ $\qquad$ $+C$
- $\int \sec u \tan u d u=$ $\qquad$ $+C$
- $\int \csc ^{2} u d u=$ $\qquad$ $+C$
- $\int \csc u \cot u d u=$ $\qquad$ $+C$
- $\quad \int \sec u d u=$ $\qquad$ $+C$
- $\int \csc u d u=$ $\qquad$ $+C$
- If $a$ is a contant and $a>0$ then $\int \frac{1}{\sqrt{a^{2}-u^{2}}} d u=\square+C$
- If $a$ is a contant and $a>0$ then $\int \frac{1}{u \sqrt{u^{2}-a^{2}}} d u=$ $\qquad$ $+C$
- Trig. Substitution: (recall that the integrand is the function you are integrating) if the integrand involves $a^{2}-u^{2}$, then one makes the substitution $u=$ $\qquad$
- Trig. Substitution:
if the integrand involves $u^{2}-a^{2}$, then one makes the substitution $u=$ $\qquad$
- Trig. Formula ... your answer should involve trig functions of $\theta$, and not of $2 \theta: \sin (2 \theta)=$ $\qquad$ .
- Trig. Formula ... $\cos (2 \theta)$ or $\sin (2 \theta)$ should appear in your answer $\cos ^{2}(\theta)=$ $\qquad$
- Trig. Formula ... $\cos (2 \theta)$ or $\sin (2 \theta)$ should appear in your answer $\sin ^{2}(\theta)=$ $\qquad$
- $\arcsin \left(-\frac{\sqrt{3}}{2}\right)=$ $\qquad$ RADIANS. (your answer should be an angle)

TABLE FOR YOUR ANSWERS TO MULTIPLE CHOICE PROBLEMS

- Indicate (by circling) directly in the table below your solution to each problem.
- You may choice up to 2 answers for each problem. The scoring is as follows. For a problem with precisely one answer marked and the answer is correct, 5 points. For a problem with precisely two answers marked, one of which is correct, 2 points. All other cases, 0 points.
- Fill in the "number of solutions circled" column. (Worth 2 points of extra credit.)


8. For the following SEQUENCES:

- if the limit exists, find it
- if the limit does not exist, then say that it DNE (which is equivalent to saying it diverges).

Put your ANSWER IN the box and show your WORK BELOW the box.
8 a.
$\lim _{n \rightarrow \infty} \frac{5 n^{2}+4 \sqrt{n}}{6 n^{2}+7 n+1}=$

8b.
$\lim _{n \rightarrow \infty} \frac{-5 n^{8}+4 \sqrt{n}}{6 n^{3}+7 n^{2}+1}=$

8 c.
$\lim _{n \rightarrow \infty} \frac{5 n^{3}+4 \sqrt{n}}{6 n^{8}+7 n^{2}+1}=$

9a. Complete the square by filling in each of the two lines with a (positive or negative) number.

$$
x^{2}-6 x+13=(x+\ldots)^{2}+
$$

9b.

$$
\int \frac{1}{\sqrt{x^{2}-6 x+13}} d x=\quad+\mathrm{C}
$$

Fall 2015
10.
$\int \frac{x^{3}+x^{2}+2 x+1}{x^{4}+2 x^{2}+1} d x=$
$+\mathrm{C}$
11. Part 11a should help with part 11b.

11a. $\int e^{\left(x^{2}\right)}(2 x) d x=\square+\mathrm{C}$

11b.We cannot integrate the functions $y=e^{x^{2}}$ and $y=x^{2} e^{x^{2}}$ with techniques we have learned thus far (in fact, they do not have elementary antiderivatives). But we can integrate $y=\left(2 x^{2}+1\right) e^{x^{2}}$ with techniques we know thus far. Evaluate $\int\left(2 x^{2}+1\right) e^{x^{2}} d x$. $\int\left(2 x^{2}+1\right) e^{x^{2}} d x=\square+\mathrm{C}$

## Honor Code Statement

I understand that it is the responsibility of every member of the Carolina community to uphold and maintain the University of South Carolina's Honor Code.
As a Carolinian, I certify that I have neither given nor received unauthorized aid on this exam.
I understand that if it is determined that I used any unauthorized assistance or otherwise violated the University's Honor Code then I will receive a failing grade for this course and be referred to the academic Dean and the Office of Academic Integrity for additional disciplinary actions.
Furthermore, I have not only read but will also follow the instructions on the exam.

Signature :

## STATEMENT OF MULTIPLE CHOICE PROBLEMS

1. Evaluate the integral

$$
\int_{0}^{1} \frac{x}{x^{2}+9} d x
$$

Hint: $\ln b-\ln a=\ln \left(\frac{b}{a}\right)$.
a. $\ln \left(\frac{10}{9}\right)$
b. $\frac{1}{2} \ln \left(\frac{10}{9}\right)$
c. $\frac{1}{2} \ln (10)-\ln (9)$
d. $2\left(\frac{10}{9}\right)$
e. None of the others.
2. Evaluate the integral

$$
\int_{0}^{4} \frac{x}{x+9} d x
$$

Hint: do you have (strictly) bigger bottoms?
a. $4-9 \ln (13)+9 \ln (9)$
b. $13-9 \ln (4)+\ln (3)$
c. $\frac{1}{9 \ln (13)}-\ln (3)$
d. $4-13 \ln (9)+3 \ln (18)$
e. None of the others.
3. Evaluate

$$
\int_{0}^{\frac{\pi}{2}} \sin ^{2} x \cos ^{3} x d x
$$

a. $\frac{3}{10}$
b. $\frac{7}{10}$
c. $\frac{8}{15}$
d. $\frac{2}{15}$
e. None of the others.
4. Evaluate the integral

$$
\int_{x=5}^{x=10} \frac{\sqrt{x^{2}-25}}{x} d x
$$

AND specify the initial substitution.
a. $\left(\sqrt{3}-\frac{\pi}{3}\right)$ using the initial substitute $x=5 \sec \theta$. b. $5\left(\sqrt{3}-\frac{\pi}{3}\right)$ using the initial substitute $x=5 \sec \theta$
c. $\left(\sqrt{3}-\frac{\pi}{3}\right)$ using the initial substitute $x=5 \sin \theta$.
d. $5\left(\sqrt{3}-\frac{\pi}{3}\right)$ using the initial substitute $x=5 \sin \theta$
e. None of the others.
5. Evaluate the integral

$$
\int_{x=1}^{x=3} \frac{5 x^{2}+3 x-2}{x^{3}+2 x^{2}} d x .
$$

a. $3 \ln 5-\ln 3-\frac{2}{3}$
b. $3 \ln 5-\ln 3-\frac{8}{3}$
c. $\ln 5-\frac{2}{3}$
d. $\frac{2}{3}-\ln 5$
e. None of the others.
6. Evaluate the integral

$$
\int_{x=-\infty}^{x=+\infty} \frac{d x}{1+x^{2}}
$$

a. $+\infty$
b. $-\infty$
c. $\pi$
d. does not exist (i.e., divergent)
e. None of the others.
7. Let $y=f(x)$ be an odd function (i.e., $f(-x)=-f(x))$ and $\int_{0}^{\infty} f(x) d x=+\infty$. What is $\int_{-\infty}^{+\infty} f(x) d x$ ?
a. $+\infty$
b. $-\infty$
c. 0
d. does not exist (i.e., divergent)
e. None of the others.

