

Test 3 Review

1. Find the interval of convergence of the Power series

$$\sum_{n=0}^{\infty} \frac{(2x-5)^n}{\sqrt{2n}}$$

2. Find the radius of convergence of the Power series

$$\sum_{n=0}^{\infty} \frac{\pi^2 (x-1)^{2n}}{(2n+1)!}$$

3. Write the Taylor series for the function centered at $x_0=1$. Write in a closed form (without "... notation)
 $F(x) = 3x^{-2}$

4. Find the Taylor series for the function
 $F(x) = \ln(1+2x)$ about the center $x_0 = 1$,

5. Represent the function $f(x) = \frac{8}{3-x}$ as a power series, then Find the largest set of x 's for which the power series converges to the function. .

6. Find a power series of $f(x) = \frac{3}{1+x^2}$ and Find the largest set of x 's for which the power series converges to the function.

7. Find the 5th order polynomial for $f(x) = \frac{7}{x}$ centered at $x_0 = -4$.

8. Use a known Taylor series to represent the integral as an infinite series, (of numbers).

$$\int_0^1 e^{-x^2} dx.$$

9. Find the power series representation of the function $f(x) = \frac{x^2}{(1-2x)^2}$. Then find the largest set of x 's for which the power series converges to the function.

$$f(x) = \frac{x^2}{(1-2x)^2}$$