

MARK BOX		
PROBLEM	POINTS	
1&2	7	
3a,b,c	20	
4a,b,c,d	33	
5	10	
take-home	30	
%	100	

NAME: _____

PIN: _____

INSTRUCTIONS:

- (1) To receive credit you must:
 - (a) **work in a logical fashion, show all your work, indicate your reasoning; no credit will be given for an answer that *just appears*;**
such explanations help with partial credit
 - (b) if a line/box is provided, then:
 - show you work BELOW the line/box
 - put your answer on/in the line/box
 - (c) if no such line/box is provided, then box your answer
- (2) The MARK BOX indicates the problems along with their points.
Check that your copy of the exam has all of the problems.
- (3) You may **not** use a calculator, books, personal notes.
- (4) During this exam, do not leave your seat. If you have a question, raise your hand. When you finish: turn your exam over, put your pencil down, and raise your hand.
- (5) This exam covers (from *Calculus* by Stewart, 6th ed., ET):
take home part 11.9–11.11 and inclass part 6.1–6.3 .

Problem Inspiration: Mostly homework and old exam problems. See the solution key for details.

Honor Code Statement

I understand that it is the responsibility of every member of the Carolina community to uphold and maintain the University of South Carolina's Honor Code.

As a Carolinian, I certify that I have neither given nor received unauthorized aid on this exam.

Furthermore, I have not only read but will also follow the above Instructions.

Signature : _____

1 & 2. Fill-in-the-blanks/boxes.

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- In 1a and 2a, fill in the blank with: perpendicular or parallel.
 - In 1b, 1c, 1d, 2b, 2c, fill in the blank with a formula involving *some of*: 2 , π , radius , radius_{big} , radius_{little} , average radius , height , and/or thickness.
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1. Disk/Washer Method

Let's say you revolve some region in the xy -plane around an axis of revolution so you get a solid of revolution. Next you want to find the volume of this solid of revolution using the disk or washer method.

1a. You should partition the coordinate axis (i.e., the x -axis or the y -axis) that is _____ to the axis of revolution.

1b. If you use the **disk method**, then the volume of a typical disk is:

_____ .

1c. If you use the **washer method**, then the volume of a typical washer is:

_____ .

1d. If you partition the z -axis, the $\Delta z =$ _____ .

2. Shell Method

Let's say you revolve some region in the xy -plane around an axis of revolution so you get a solid of revolution. Next you want to find the volume of this solid of revolution using the shell method.

2a. You should partition the coordinate axis (i.e., the x -axis or the y -axis) that is _____ to the axis of revolution.

2b. If you use the **shell method**, then the volume of a typical shell is:

_____ .

2c. If you partition the z -axis, the $\Delta z =$ _____ .

3. Let R be the region enclosed by

$$y = x^2 \quad \text{and} \quad y = x + 2 .$$

Let A be the area of the region R .

3a. The points of intersection of $y = x^2$ and $y = x + 2$ are $P = (\text{____} , \text{____})$ and $Q = (\text{____} , \text{____})$.
Make a rough sketch of the region R , labeling P and Q .

3b. Express the area A as integral(s) with respect to x (so you want dx).

You do NOT have to evaluate the integral(s) nor do lots of algebra.

A =

3c. Express the area A as integral(s) with respect to y (so you want dy).

You do NOT have to evaluate the integral(s) nor do lots of algebra.

A =

4. Sketched below is the region R that is enclosed by

$$y = 3x^2 \quad \text{and} \quad y = 0 \quad \text{and} \quad x = 1 \quad \text{and} \quad x = 2 .$$

4a. In the sketch below, draw in a typical rectangle (should it be horizontal or vertical?) that would be used to express the area of R as precisely 1 integral (and not 2 integrals).

►. In each of problems 4b, 4c, 4d:

- R will be revolved around some line to create a solid of revolution
- using either the disk, washer, or shell method, express the volume V of the resulting solid of revolution as **one integral** (and NOT as 2 or more integrals).
- In the space provided **below** each problem, make some *good enough sketch* (does not have to be too fancy) to indicate (i.e., help justify) your thinking/reasoning behind your solution
- you do not have to do lots of algebra to your integrand
- you do not have to integrate your integral.

4b. The volume V of the solid obtained by revolving the region R about the x -axis is

$V =$

4c. The volume V of the solid obtained by revolving the region R about the y -axis is

$V =$

4d. The volume V of the solid obtained by revolving the region R about the **horizontal** line $y = 12$ is

$V =$

5. Using the disk/washer method, express as an integral (do not evaluate) the volume of a frustum of a right circular cone with height h , lower base radius R , and top radius r .

$V =$

5. Using the disk/washer method, express as an integral (do not evaluate) the volume of a cap of a sphere with radius r and height h .

V =