MATH 550 Section 001 Fall 2005 Bonus Project 2

(Due in Class November 17)

Let a be the largest digit among the last four digits of your student number and b be the smallest positive digit. Consider the triple integral

$$\iiint_W z^2 e^{x^2 + y^2} \, dx \, dy \, dz$$

where W is the region in the first octant $(x \ge 0, y \ge 0, z \ge 0)$ bounded by the surfaces $x = 0, y = 0, x^2 + y^2 + z^2 = a, x^2 + y^2 + z^2 = b$ and $x^2 + y^2 = z^2$.

- (a) Plot the region W. (Helpful Maple commands: with(plots), plot3d, display.)
- (b) Find a numerical value for the integral. (Helpful Maple commands: int, evalf. More information on numerical integration can be found under int[numerical].)

Your solution should include several plots for (a) and the answer to (b), with detailed explanations of how you obtained your answer. You should include a neat Maple worksheet containing the relevant computations.