# New Functions from Old

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# Overview

In this lab, we will use Maple to help us to calculate and simplify combinations of functions. A maplet (**Shift**) will also be introduced to help us to practice our skills identifying basic functions that have been shifted horizontally and/or vertically.

# Maple Essentials

• Important Maple commands introduced in this lab:

Command	Description	Example
:=->	define a function in x	f:=x->2*x^2*(1-x^2);
simplify	simplify functions/expressions	<pre>simplify(f(x));</pre>
		<pre>simplify(x-(x-1)^8);</pre>
eval	evaluate functions/expressions	<pre>eval(f(x),x=2);</pre>
		eval((x-h)^9,h=0);

• The **Shift** maplet is available from the course website:

 $\texttt{http://people.math.sc.edu/calclab/141L-S19/labs/} \rightarrow \underline{Shift}$ 

# Related course material/Preparation

 $\S{1.2.}$ 

# Assignment

Complete lab activities and your lab instructor will give other assignment for each section

# Activities

- 1. Use the **Shift** maplet to practice your skills identifying basic functions that have been shifted horizontally and/or vertically.
  - (a) From the Calculus I Suggested Lab Schedule/Assignments page under Lab 2, click on <u>Shift</u>. You will be prompted for a username and password as these maplets are protected. You should use your Blackboard username and password. (You may need to reset your password there: login to your VIP, go to the TECHNOLOGY, choose the second one from the TECHNOLOGY Menu.)
  - (b) This opens a user interface for testing your ability to recognize shifts of seven basic functions. To see the seven basic functions, click the **Show Basic 7 Functions** button.
  - (c) To test your ability to recognize shifts of these functions, click on the **Show Shifted Graph** button. Enter the formula for the displayed graph (using valid Maple syntax) in the box labeled *Answer*, then click the **Check Answer** button.

Note: If you do not get the answer correct, the graph of your equation will be displayed in red.

2. In each of the following problems, you will use the assignment operator (:=) together with the arrow notation (x->) to define each function. Once you have done this, the problems are straightforward. Remember that you have to call a function **together with its variable** (like f(x), f(t), f(2), or f(whatever)). Maple won't recognize a function just by his name (like f).

**Note:** You can always use the Expression, Common Symbols, and/or Favorites palettes to avoid typing so much. You may also find the labels useful.

- Find and simplify formulas for f(x) + g(x), f(x) g(x), f(x)g(x), and f(x)/g(x). a.  $f(x) = 2\sqrt{x-1}$ ,  $g(x) = \sqrt{x-1}$ b.  $f(x) = 1 + \frac{x}{x+1}$ ,  $g(x) = 2 - \frac{1}{x}$
- Let  $f(x) = x^2 + 1$ . Find and simplify each of the following. a. f(5s+2) b. 3f(1/x) c. f(f(x))
- Evaluate  $\frac{f(x+h)-f(x)}{h}$ . Simplify your answer and then let h go to 0. a.  $f(x) = 3x^2 - 5$  b.  $f(x) = \frac{1}{(x+1)^2}$
- Find and simplify compositions  $(f \circ g)(x) = f(g(x))$  and  $(g \circ f)(x) = g(f(x))$ . a.  $f(x) = \frac{1+x}{1-x}$ ,  $g(x) = \frac{x}{1-x}$ b.  $f(x) = \sqrt{2x+3}$ ,  $g(x) = x^2 + 1$
- Find and simplify (f ∘ g ∘ h)(x).
  a. f(x) = √x − 1, g(x) = x<sup>2</sup> + 2, h(x) = cos x
  b. f(x) = x<sup>2</sup> + 1, g(x) = <sup>1</sup>/<sub>x</sub>, h(x) = x<sup>3</sup>
- Express F(x) as a composition of two functions; that is, find f(x) and g(x) such that F(x) = f ∘ g(x). Use Maple to verify the composition.
  Note: Do not choose the identity (y = x) as one of your functions.
  a. F(x) = sin<sup>2</sup> x
  b. F(x) = 3/(5+cos x) c. F(x) = (x<sup>2</sup> + 1)<sup>10</sup>
- Express F(x) as a composition of three functions; that is, find f(x), g(x), and h(x) such that  $F = f \circ g \circ h(x)$ . Use Maple to verify the composition. **Note:** Do not choose the identity (y = x) as one of your functions. a.  $F(x) = (1 + \sin(x^2))^3$  b.  $F(x) = \sqrt{1 - x^{1/3}}$  c.  $F(x) = \cos^4(\sqrt{x})$

#### Example Problems

- 1. Evaluate the difference quotient  $\frac{f(x+h)-f(x)}{h}$ ,  $h \neq 0$  if  $f(x) = \frac{4}{3+x^2}$ . Simplify your answer and then let h go to 0.
  - > f:= x -> 4 /  $(3+x^2);$
  - > (f(x+h) f(x)) / h;
  - > simplify(label);
  - > eval(*label*, [h = 0, x = x]);

**Note:** You should right-click over your expression and choose an action. If you choose to type the command, use **Ctrl-L** to insert a label.

- 2. Find and simplify  $f \circ g \circ h(x)$  if  $f(x) = \frac{2}{1-x^2}$ ,  $g(x) = \sin(x)$ , and  $h(x) = \sqrt{x}$ .
  - > f:= x -> 2 / (1- $x^2$ );
  - > g:= x -> sin(x);
  - > h:= x -> sqrt(x);
  - > f(g(h(x)));
  - > simplify(label);