New Functions from Old

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Overview

In this lab, we will use Maple to help us to calculate and simplify combinations of functions. A maplet (**Shift**) will also be introduced to help us to practice our skills identifying basic functions that have been shifted horizontally and/or vertically.

Maple Essentials

• Important Maple commands introduced in this lab:

Command	Description	Example
:=->	define a function in x	f:=x->2*x^2*(1-x^2);
simplify	simplify functions/expressions	<pre>simplify(f(x));</pre>
		$simplify(x-(x-1)^8);$
eval	evaluate functions/expressions	eval(f(x),x=2);
		eval((x-h)^9,h=0);

• The **Shift** maplet is available from the course website:

 $\texttt{http://people.math.sc.edu/calclab/141L-S17/labs/} \rightarrow \underline{\textbf{Shift}}$

Related course material/Preparation

§1.2.

Assignment

Complete lab activities and your lab instructor will give other assignment for each section

Activities

- 1. Use the **Shift** maplet to practice your skills identifying basic functions that have been shifted horizontally and/or vertically.
 - (a) From the Calculus I Suggested Lab Schedule/Assignments page under Lab 2, click on Shift. You will be prompted for a username and password as these maplets are protected. You should use your Blackboard username and password. (You may need to reset your password there: login to your VIP, go to the TECHNOLOGY, choose the second one from the TECHNOLOGY Menu.)
 - (b) This opens a user interface for testing your ability to recognize shifts of seven basic functions. To see the seven basic functions, click the **Show Basic 7 Functions** button.
 - (c) To test your ability to recognize shifts of these functions, click on the **Show Shifted Graph** button. Enter the formula for the displayed graph (using valid Maple syntax) in the box labeled *Answer*, then click the **Check Answer** button.

Note: If you do not get the answer correct, the graph of your equation will be displayed in red.

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2. In each of the following problems, you will use the assignment operator (:=) together with the arrow notation (x->) to define each function. Once you have done this, the problems are straightforward. Remember that you have to call a function together with its variable (like f(x), f(t), f(t), or f(t) whatever). Maple won't recognize a function just by his name (like f).

Note: You can always use the Expression, Common Symbols, and/or Favorites palettes to avoid typing so much. You may also find the labels useful.

- Find and simplify formulas for f(x) + g(x), f(x) g(x), f(x)g(x), and f(x)/g(x). a. $f(x) = 2\sqrt{x-1}$, $g(x) = \sqrt{x-1}$ b. $f(x) = 1 + \frac{x}{x+1}$, $g(x) = 2 - \frac{1}{x}$
- Let $f(x) = x^2 + 1$. Find and simplify each of the following. b. 3f(1/x)c. f(f(x))
- Evaluate $\frac{f(x+h)-f(x)}{h}$. Simplify your answer and then let h go to 0. a. $f(x) = 3x^2 5$ b. $f(x) = \frac{1}{(x+1)^2}$
- Find and simplify compositions $(f \circ g)(x) = f(g(x))$ and $(g \circ f)(x) = g(f(x))$. a. $f(x) = \frac{1+x}{1-x}$, $g(x) = \frac{x}{1-x}$
 - b. $f(x) = \sqrt{2x+3}, \ g(x) = x^2 + 1$
- Find and simplify $(f \circ g \circ h)(x)$. a. $f(x) = \sqrt{x - 1}$, $g(x) = x^2 + 2$, $h(x) = \cos x$ b. $f(x) = x^2 + 1$, $g(x) = \frac{1}{x}$, $h(x) = x^3$
- Express F(x) as a composition of two functions; that is, find f(x) and g(x) such that $F(x) = f \circ g(x)$. Use Maple to verify the composition.

Note: Do not choose the identity
$$(y=x)$$
 as one of your functions.
a. $F(x)=\sin^2 x$ b. $F(x)=\frac{3}{5+\cos x}$ c. $F(x)=(x^2+1)^{10}$

• Express F(x) as a composition of three functions; that is, find f(x), g(x), and h(x)such that $F = f \circ g \circ h(x)$. Use Maple to verify the composition.

Note: Do not choose the identity (y = x) as one of your functions.

a.
$$F(x) = (1 + \sin(x^2))^3$$
 b. $F(x) = \sqrt{1 - x^{1/3}}$ c. $F(x) = \cos^4(\sqrt{x})$

Example Problems

- 1. Evaluate the difference quotient $\frac{f(x+h)-f(x)}{h}$, $h \neq 0$ if $f(x) = \frac{4}{3+x^2}$. Simplify your answer and then let h go to 0.
 - $> f := x -> 4 / (3+x^2);$ > (f(x+h) - f(x)) / h;> simplify(label);

> eval(label, [h = 0, x = x]);

Note: You should right-click over your expression and choose an action. If you choose to type the command, use Ctrl-L to insert a label.

2. Find and simplify $f \circ g \circ h(x)$ if $f(x) = \frac{2}{1-x^2}$, $g(x) = \sin(x)$, and $h(x) = \sqrt{x}$. $> f := x \rightarrow 2 / (1-x^2);$ $> g:= x \rightarrow sin(x);$ > h:= x -> sqrt(x); > f(g(h(x)));> simplify(label);

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