1. { 10 points } Let $f : \mathbb{R} \rightarrow \mathbb{R}$ and let $f(x) < 0$ for all $x \in \mathbb{R}$. Prove that $f(x)$ is strictly increasing if and only if the function $g(x) = \frac{1}{f(x)}$ is strictly decreasing.